

Thermodynamic scaling of the viscosity of van der Waals, H-bonded, and ionic liquids

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Viscosities η and their temperature T and volume V dependences are reported for seven molecular liquids and polymers. In combination with literature viscosity data for five other liquids, we show that the superpositioning of relaxation times for various glass-forming materials when expressed as a function of TV^γ , where the exponent γ is a material constant, can be extended to the viscosity. The latter is usually measured to higher temperatures than the corresponding relaxation times, demonstrating the validity of the thermodynamic scaling throughout the supercooled and higher T regimes. The value of γ for a given liquid principally reflects the magnitude of the intermolecular forces (e.g., steepness of the repulsive potential); thus, we find decreasing γ in going from van der Waals fluids to ionic liquids. For some strongly H-bonded materials, such as low molecular weight polypropylene glycol and water, the superpositioning fails, due to the nontrivial change of chemical structure (degree of H bonding) with thermodynamic conditions. © 2006 American Institute of Physics. [DOI: 10.1063/1.2346679]

INTRODUCTION

Identifying the intermolecular potential governing the interactions in liquids is central to understanding their thermodynamic and other properties. This statement is especially pertinent for the supercooled regime, in which the mobility of viscous liquids is governed by (infrequent) jumps over large barriers in comparison with the available thermal energy. However, due to the cooperativity inherent to vitrifying liquids, each molecule is involved with competing interactions with many neighbors, and an interpretation requires consideration of the complex topography of the multidimensional potential energy landscape.¹⁻⁶ One simplification is to approximate the interactions with a spherically symmetric, pairwise additive, repulsive potential,⁷⁻⁹

$$U(r) \sim \left(\frac{\sigma}{r}\right)^{3\gamma}, \quad (1)$$

where r is the intermolecular separation, and σ and γ are material-specific constants related, respectively, to the molecular size and the steepness of the potential. There is no explicit consideration of attractive forces, since condensation/solidification is primarily driven by the repulsive forces.¹⁰⁻¹²

Equation (1) implies that the product of the glass transition temperature T_g times the specific volume V , raised to the power of γ , will be a constant. This was verified in molecular dynamic simulations (MDSs) of a Lennard-Jones (LJ) fluid

($3\gamma=12$), for which the quantity $T_g V_g^4$ (V_g is the specific volume at the glass transition) was found to be independent of pressure.^{13,14} A similar result was obtained from quasielastic neutron scattering on o-terphenyl (OTP) by Tolle *et al.*¹⁵ for the dynamic crossover temperature of mode coupling theory. Subsequently, Hollander and Prins,¹⁶ determined by NMR measurements at high pressures that $T_g V_g^2$ was constant for atactic polypropylene, the smaller value of γ reflecting the softer potential for the polymer (as discussed below).

The constancy of the product $T_g V_g^\gamma$ follows from the fact that the relaxation time at T_g is constant.¹⁷ Thus, the invariance of $T_g V_g^\gamma$ can be generalized to all relaxation times by superimposing $\tau(T, P)$ vs TV^γ ; that is, τ is a unique function of TV^γ ,

$$\tau(T, V) = \mathcal{J}(TV^\gamma), \quad (2)$$

as first shown for OTP with $\gamma=4$,¹⁸⁻²⁰ and subsequently for a wide range of glass-forming liquids and polymers ($0.13 \leq \gamma \leq 8.5$) by dielectric spectroscopy,²¹⁻²⁷ light scattering,²⁸ and mds.^{29,30} Equation (2) also applies to polymer blends, with each component exhibiting a unique value of γ .^{31,32} Furthermore, since the scaling exponent can be deduced from PVT measurements³³ or identified with the Grüneisen parameter,^{34,35} the scaling relation [Eq. (2)] enables the volume and pressure dependences of τ to be determined from relaxation measurements made only at atmospheric pressure. The parameter γ has been found to correlate with the steepness index (fragility³⁶) at atmospheric pressure³⁷ and ultimately with the general T dependence.³⁸

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In addition to providing a means to characterize relaxation times of glass formers, the appeal of the scaling is its putative connection to the intermolecular potential. The form of Eq. (1) is expected to apply to van der Waals or other liquids lacking strong specific interactions; nevertheless, hydrogen-bonded liquids such as sorbitol²¹ and glycerol^{26,27} conform to Eq. (2). It is surprising that the relaxation times for a liquid whose chemical structure is sensitive to temperature (and perhaps pressure^{39–42}) would superpose for a constant value of γ . We examine this further herein, considering data for polypropylene glycol and water, nonspherical molecules with extensive, directional hydrogen bonding.

Along these same lines, it is of interest to determine if the relaxation properties of ionic liquids can be described using Eq. (2). Ionic liquids are molten organic salts, usually with low (<100 °C) melting points. They find increasing applications, for example, as substitutes for traditional solvents, due to their good dissolution properties, high thermal stability, and negligible vapor pressure under ambient conditions.⁴³ The interactions in these polar, noncoordinating liquids are complex, entailing electrostatic as well as van der Waals bonding. Viscosity η and PVT measurements have been carried out at elevated pressures for three ionic liquids,^{44,45} and these data allow assessment of the applicability of the thermodynamic scaling. The viscosity is an especially important property of ionic liquids since it governs the diffusivity and thus rate of chemical reactions carried out in an ionic liquid medium. To date, viscosity scaling has only been applied to results for OTP,²⁴ glycerol,²⁸ and salol⁴⁶ with the obtained exponents close to the γ from relaxation measurements.^{18,26,27} Approaching the glass transition, η of a liquid increases by many orders of magnitude over a small temperature range, mirroring the behavior of the structural relaxation time. According to the Einstein-Debye relation,^{47,48}

$$\eta = \left(\frac{kT}{v_m} \right) \tau, \quad (3)$$

where v_m is the molecular volume. This equation was derived originally for Brownian particles, which are larger than molecules. An analogous relation is the Maxwell equation⁴⁹

$$\eta = G_\infty \tau, \quad (4)$$

where G_∞ is the infinite-frequency (glassy) shear modulus of the liquid. These equations are commonly used both for liquids and for probe molecules dispersed in a fluid. As the glass transition temperature is approached from above, Eq. (4) is found to underestimate the viscosity,^{50–52} a phenomenon referred to as decoupling. Herein we analyze results, primarily viscosity data, for various liquids. These range from simple organic molecules and higher molecular weight compounds (including, for example, a perfluorinated polyalkylether used in various applications such as computer hard drives, uranium enrichment centrifuges, and jet engines)

to associated liquids and molten salts. From these data we assess the general applicability of Eq. (2).

EXPERIMENT

Viscosities were measured using three falling-ball viscometers.^{53,54} PVT data were obtained with either a metal bellows piezometer⁵⁵ or a commercial Gnomix instrument, which uses a similar bellows with the sample confined in mercury.⁵⁶ The perfluoropolyether (PFPE) was Fomblin Z25 from Solvay Solexis Inc. It is a linear copolymer of $(-\text{CF}_2-\text{CF}_2-\text{O}-)$ and $(-\text{CF}_2-\text{O}-)$ in the ratio of ~ 0.65 , with terminal CF_3 groups. The molecular weight was 9.5 kg/mol (~ 95 repeat units per chain). The 1,1-(1,1,3-trimethyl-1,3-propanediyl)bis-cyclohexane (BCH, $M_w=250$ g/mol) was obtained from Sigma Aldrich. The *p*-bis(phenylethyl) benzene (BPEB, $M_w=286$ g/mol) was from Monsanto. The squalane (hexamethyltetracosane) was obtained from Sigma-Aldrich and had a molecular weight $M_w=422.8$ g/mol (seven repeat units). The mineral oil was LVI 260 from Shell Lubricants with $M_w \sim 425$ g/mol.⁵⁷ The polyglycol (Sigma-Aldrich) was a random copolymer of 75% (by weight) ethylene- and 25% propylene-glycol (4:1 mole ratio), hydroxyl terminated with $M_w=12.5$ kg/mol (45 repeat units). Dibutylphthalate was obtained from Sigma-Aldrich.

Literature data were analyzed herein for octane,⁵⁸ toluene,⁵⁸ water,^{59,60} and three ionic liquids. 1-butyl-3-methylimidazolium hexafluorophosphate,⁴⁴ 1-methyl-3-octylimidazolium tetrafluoroborate,⁴⁵ and 1-methyl-3-octylimidazolium hexafluorophosphate.⁴⁵ Ionic liquids are very hygroscopic; the reported measurements were obtained on dry samples [water content <60 ppm (Ref. 45)]. The chemical structures of all materials are displayed in Table I.

RESULTS AND DISCUSSION

Nonassociated liquids

The interaction potential underlying the scaling is most obviously appropriate for nonassociated glass formers; accordingly, in Fig. 1 the scaling of viscosity data⁵⁸ is shown for octane, a prototypical van der Waals liquid. Isotherms for pressures over the range from 0.1 to ~ 370 MPa superpose when plotted versus TV^γ , demonstrating the extension of the thermodynamic scaling, previously applied to relaxation times, to η . The large value of γ for octane reflects a strong volume contribution to the dynamics. We also note that the curvature of the octane data indicates an increase in the variation of η with decreasing TV^γ ; this differs from the usual behavior.¹⁷ Since heretofore the scaling was investigated mainly for much larger τ (i.e., larger η), it is not clear if this is a true exception. Also in the figure are viscosity data for toluene,⁵⁸ which are more nearly Arrhenius and characterized by a slightly smaller $\gamma=7.5$. Interactions arising from the polarizable phenyl group are expected to emphasize the effect of temperature relative to that of volume. Thus, viscosities for BPEB, a model lubricant⁶¹ having three benzene

TABLE I. Materials and scaling exponents.

	chemical name	structure	γ
octane	n-octane		8.0
toluene	toluene		7.5
BCH	1,1-(1,1,3-trimethyl-1,3-propanediyl)bis-cyclohexane		7.5
PFPE	perfluoropoly(ethyleneoxide-ran-methyleneoxide)	$\text{CF}_3(-\text{CF}_2-\text{CF}_2-\text{O})_x(-\text{CF}_2-\text{O})_y-\text{CF}_3$	6.0
BPEB	p-bis(phenylethyl)benzene		4.8
squalane	2,6,10,15,19,23-hexamethyltetracosane		4.2
mineral oil	linear and cyclic alkanes	NA	4
polyglycol	poly(ethylene glycol-ran-propylene glycol)	$\text{HO}(-\text{CH}_2-\text{CH}_2-\text{O})_x(-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{O})_y-\text{H}$	2.3
DBP	di-n-butylphthalate		3.2
water	water		---
[OMIM]BF ₄	1-methyl-3-octylimidazolium tetrafluoroborate		2.25
[OMIM]PF ₆	1-methyl-3-octylimidazolium hexafluorophosphate		2.4
[BMIM]PF ₆	1-butyl-3-methylimidazolium hexafluorophosphate		2.9

rings, superpose for an even smaller value of $\gamma=4.8$ (Fig. 2).

Viscosity master curves for two other nonpolar liquids, BCH and PFPE, are also shown in Fig. 2. For the former $\gamma=7.5$, which is quite similar to the behavior of the simpler organic liquids in Fig. 1. For the PFPE, however, superpositioning of η requires a smaller scaling exponent=6.0. Although not a large difference, this reduced volume dependency is a consequence of the long chain character of PFPE, i.e., the greater concentration of intramolecular bonds. Equation (1), which serves as the putative basis for the thermody-

amic scaling, does not describe intramolecular bonding. A harmonic potential is more appropriate for changes in covalent bond lengths and angles arising from volume changes.^{62,63} These intramolecular bonds thus serve to soften the potential.

This effect was seen in a recent mds of 1,4-polybutadiene by Tsolou *et al.*³⁰ These authors employed an LJ 6-12 intermolecular potential in combination with harmonic backbone bonds to characterize the forces between chain segments.⁶³ The chain mobility data (both segmental and normal mode dynamics) for different T and V super-

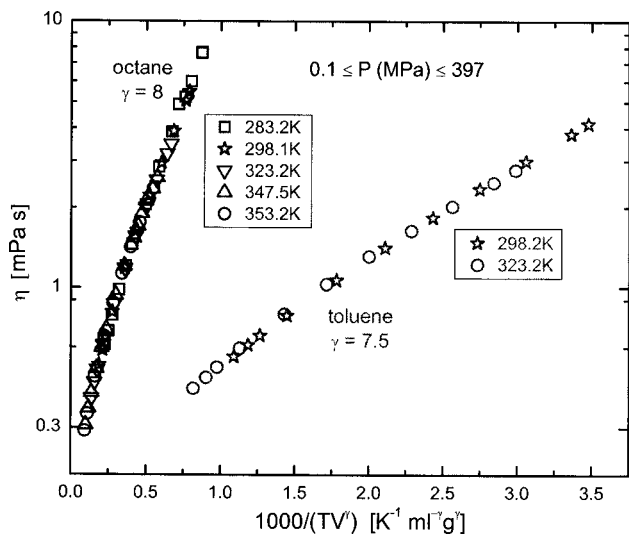


FIG. 1. Superpositioned viscosities of octane and toluene, with $\gamma=8.0$ and 7.5 , respectively. The η were taken from Ref. 58, with isotherms reported over the indicated pressure range and each symbol type representing a different measurement temperature.

posed according to Eq. (2) with $\gamma=2.8$.³⁰ This is smaller than the value of 4 expected for the LJ potential ($r^{12} \sim V^4$), reflecting the influence of the intramolecular bonds. We illustrate this effect in Fig. 3, showing the intermolecular potential resulting from a LJ 6-12 interaction between non-bonded atoms in combination with harmonic chain backbone stretching,

$$U(r) \sim \varepsilon \left[\left(\frac{\sigma}{r} \right)^{12} - 2 \left(\frac{\sigma}{r} \right)^6 \right] + k(r-l)^2. \quad (5)$$

In calculating the potential shown in the figure, we used average values for the three carbon-carbon bonds:⁶³ the LJ

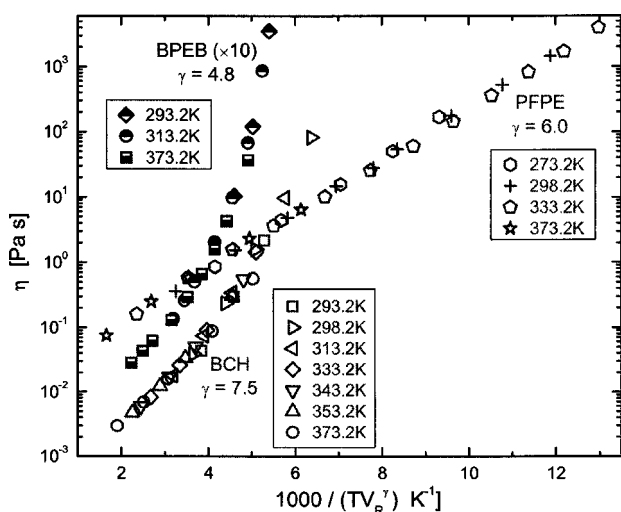


FIG. 2. Superpositioned viscosities of *p*-bis(phenylethyl)benzene ($\gamma=4.8$), perfluoropolyether ($\gamma=6.0$), and 1,1-(1,1,3-trimethyl-1,3-propanediyl)biscyclohexane ($\gamma=7.5$). The range of pressures was from ambient to 610 MPa (BPEB), 1180 MPa (PFPE), and 300 MPa (BCH). Different symbols represent the different measurement temperatures of each isotherm (note that the viscosities of BPEB were shifted upward by one decade for clarity). Volumes V_R are relative values.

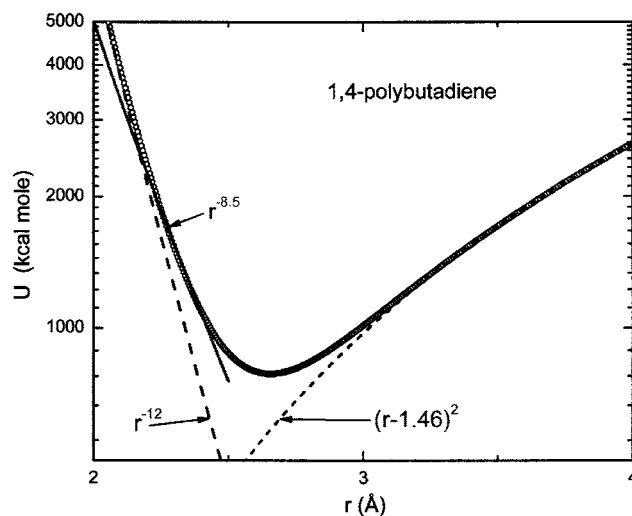


FIG. 3. Intermolecular potential for 1,4-polybutadiene calculated as the sum of an LJ 6-12 intermolecular potential and a harmonic intramolecular bond stretching potential [Eq. (5)]. The parameters were taken from Ref. 63, with average values used for the interaction parameters. The solid line is the fit to the repulsive energy in the vicinity of the minimum, the long dashed line represents the limiting value of the repulsive energy at small r , and the short dashed line is the bond stretching interaction.

energy parameter $\varepsilon=0.984$ kcal/mol, LJ length scale parameter $\sigma=4.19$ Å, the backbone force constant $k=821$ kcal/(mol Å²), and backbone bond length $l=1.46$ Å. While the asymptote at small r indeed reflects the value of the exponent 12 in Eq. (5), in the vicinity of the local minimum the repulsive interaction is softer, describable by a power law $r^{-8.5}$. This same effect—a reduction in steepness of the repulsive potential due to a surfeit of intramolecular bonds—likely underlies the fact that superpositioning of dielectric relaxation times for polymers entails smaller γ than the scaling exponent for molecular liquids.^{17,22} Note that because of the extensive intramolecular bonding, chain compaction *per se* makes a small (or negligible) contribution to the bulk compressibility of polymers;^{64,65} thus, volume effects are deemphasized and the observed γ is reduced.

Squalane is a saturated polybutene of modest molecular weight. Using the equation of state reported by Fandino *et al.*,⁶⁶ a master curve for η of squalane is obtained with $\gamma=4.2$ (Fig. 4). Mineral oil, an oligomeric hydrocarbon mixture of branched and linear alkanes and aliphatic and aromatic rings, exhibits behavior which is slightly less volume dependent, $\gamma=4.0$ (Fig. 4). The exponents for both liquids are significantly smaller than the values for the van der Waals molecular liquids in Figs. 1 and 2 and the polymer, PFPE (Fig. 2). The latter demonstrates the effect of backbone structure. Although it is not possible to make a direct connection between chemical structure and γ , PFPE is nonpolar and a very flexible polymer, having a facily rotating ether linkage in every repeat unit. In the same manner that a flexible chain structure lowers the glass transition temperature (by mitigating constraints on the many-body dynamics⁶⁷), the large value of γ for PFPE (in comparison to the

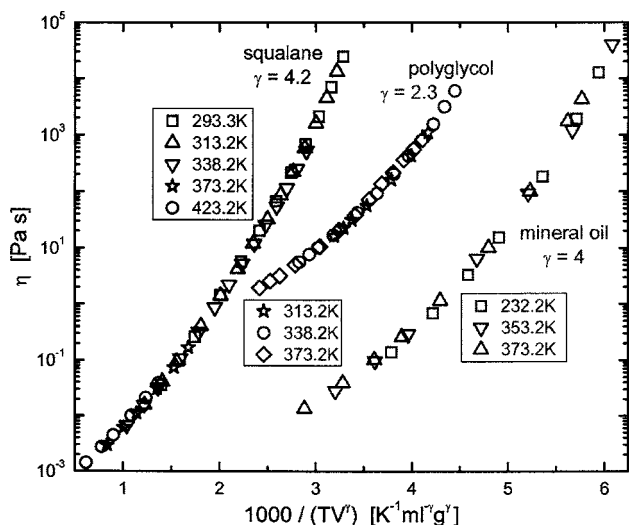


FIG. 4. Superpositioned viscosities of polyglycol ($\gamma=2.3$), mineral oil ($\gamma=4.0$), and squalane ($\gamma=4.2$). The range of pressure for the measurements was from ambient to 1000 MPa (polyglycol), 1200 MPa (squalane), and 633 MPa (mineral oil). Different symbols represent different measurement temperatures.

oligomers in Fig. 4 and general results for polymers^{17,22}) reveals a similar effect on the V dependence of η .

To examine the connection between the interaction strength and the scaling exponent, we analyze data for a

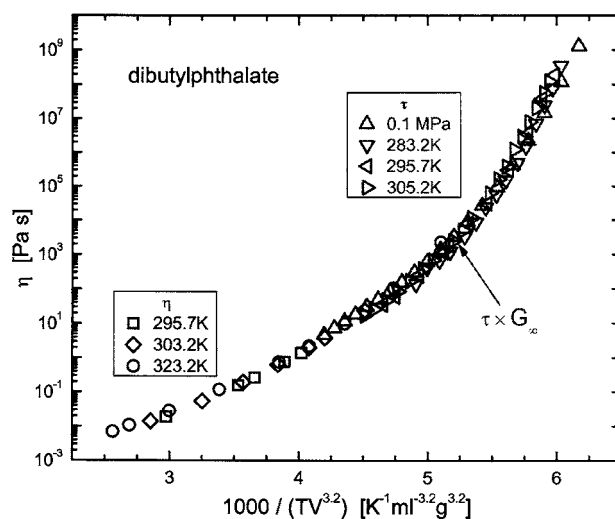


FIG. 5. Superpositioned viscosities of dibutylphthalate with $\gamma=3.2$. The measurement pressure was from 0.1 to 1250 MPa at various temperatures as denoted by the symbol type. Dielectric relaxation times (Ref. 69) for $P \leq 1610$ MPa are included in the figure after multiplication by a factor of 2×10^8 Pa.

polar molecule [dipole moment=2.4 D Ref. 68], dibutylphthalate (DBP). The measured temperature and pressure dependences of the liquid specific volume were fit to the Tait equation, yielding

$$V(T, P) = (1.0255 + (6.79 \times 10^{-4}T) + (6.28 \times 10^{-7}T^2)) \times \left[1 - 0.0894 \ln \left(1 + \frac{P}{203.1 \exp(-4.619 \times 10^{-3}T)} \right) \right], \quad (6)$$

with units of ml/g for V , and P and T in MPa and Celsius, respectively. As seen in Fig. 5, the viscosity data collapse for DBP onto a single master curve when plotted as a function of $TV^{3.2}$. This is a very small value of the exponent; in fact, DBP exhibits the lowest γ found to date for any molecular glass-former lacking hydrogen bonds.¹⁷ Since a dipole-dipole interaction would increase the intensity of the attractive term of the potential, it is tempting to infer that the polarity in DBP could soften the effective repulsive interactions (similar to the effect of intrachain potential shown in Fig. 3). This would minify the contribution of volume to the dynamics relative to the influence of temperature. Certainly this is an intriguing avenue for future experiments.

Also included in Fig. 5 are dielectric relaxation times for DBP measured at ambient and elevated pressures.⁶⁹ The relaxation times also scale for the same value of $\gamma=3.2$; moreover, using Eq. (4) with $G_\infty=0.2$ GPa, the τ superpose onto the viscosity data. This value of G_∞ is close to acoustic determinations of the high frequency shear modulus, $=0.33$ GPa.⁷⁰ The combined superpositioning of η and τ demonstrates that for a constant value of γ the thermody-

amic scaling applies over a broad dynamic range (almost 12 decades—encompassing the dynamic crossover³³).

H-bonded materials

Hydrogen-bonded liquids are strongly associated, and thus volume exerts a weak effect on their dynamics.^{17,71,72} Furthermore, if hydrogen bond dissociation occurs with temperature (or in response to pressure^{39–41}), the dynamics should depart from the thermodynamic scaling, since the chemical structure of the fluid is varying with T and P . Nevertheless, relaxation times for at least some H-bonded liquids such as sorbitol [$\gamma=0.13$ (Ref. 21)] and glycerol [$\gamma=1.6 \pm 0.2$ (Refs. 26–28)] do conform to Eq. (2). Since $\gamma=0$ means that η and τ are a functions of T alone, the value of γ for sorbitol indicates an almost negligible role of volume. However, any change of H bonding with thermodynamic conditions is evidently insufficient to cause breakdown of the TV^γ scaling. Relaxation times for weakly associated polymers such as polypropylene glycol (with $M_w=4$ kg/mol only two of the 69 repeat units, the terminal end ones, form hydrogen bonds) also superpose as a function

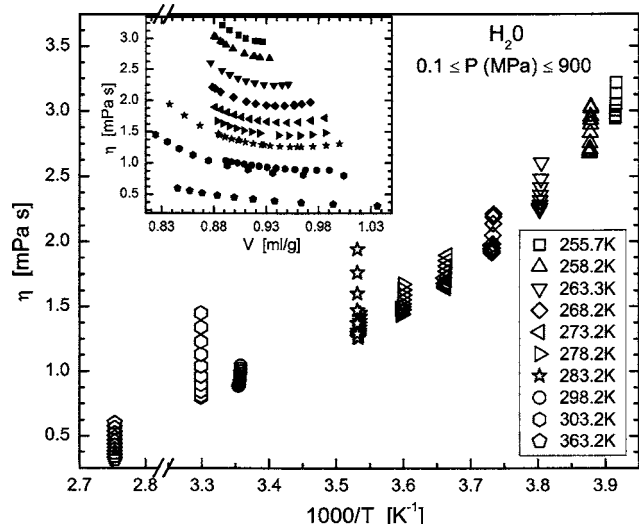


FIG. 6. Arrhenius plots of the viscosity of water, indicating that temperature is the dominant control variable. Each symbol represents an isotherm of $\eta(P)$ for P from ambient up to as much as 900 MPa. The inset is the same data as a function of specific volume, showing the negligible V dependence and the weak minimum related to the H-bond network structure. Collapse of the data to form a master curve when plotted versus TV^γ was not observed for any value of the exponent γ . The η were taken from Refs. 59 and 60.

of TV^γ .⁷³ Generally, for polymers with terminal hydroxyl groups, the influence of volume increases with molecular weight,⁷⁴ presumably a reflection of decreased H bonding.

Figure 4 shows the viscosities for a polyglycol with $M_w=12.5$ kg/mol. The η measured at three pressures collapse to a single curve for $\gamma=2.3$. This value of the exponent is slightly less than for polypropylene glycol having lower M_w , for which $\gamma=2.5$.⁷³ For low enough molecular weights (and thus more terminal hydroxyl groups), the H bonding is sufficient to cause a breakdown of the superpositioning. For example, we find that dielectric relaxation data for polypropylene glycol with $M_w=0.4$ kg/mol (seven repeat units)^{56,75} and lower⁷⁴ do not superpose versus TV^γ (data not shown).

The most common H-bonded liquid is water, which can form up to four hydrogen bonds per molecule. This number varies with temperature^{76,77} and pressure,³⁹ so that a breakdown of the thermodynamic scaling is expected. The inset to Fig. 6 shows the viscosity of water from $T=255$ to 363 K for pressures up to 900 MPa.^{59,60} The η exhibit a minimum as a function of the specific volume, in accord with the temperature dependences of various thermodynamic properties of water such as the density, heat capacity, and compressibility, which likewise go through a minimum in the vicinity of $T \sim 300$ K.⁷⁸ This behavior is a consequence of the hydrogen bonds, specifically the geometrical constraints imposed by their formation. Directional interactions among water molecules give rise to an open H-bond structure, having a lower density and different properties than unassociated water molecules. The formation of this H-bond network is enhanced for a particular T -dependent volume⁷⁸ and this dependence of the chemical structure on thermodynamic conditions precludes a description of the viscosities as a unique function of TV^γ . The countervailing effects of pressure (volume)—greater congestion reducing mobility while disruption of H-bonding increases mobility—results in an extremely weak

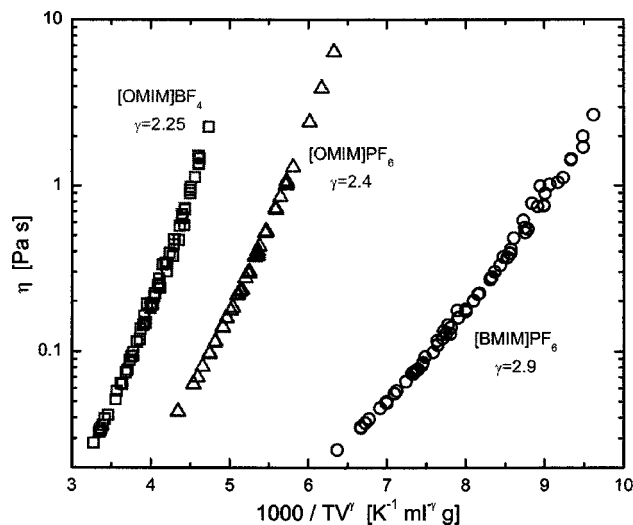


FIG. 7. Superpositioned viscosities of the ionic liquids: 1-methyl-3-octylimidazolium tetrafluoroborate ($\gamma=2.25$), 1-methyl-3-octylimidazolium hexafluorophosphate ($\gamma=2.4$), and 1-butyl-3-methylimidazolium hexafluorophosphate ($\gamma=2.9$). The data were taken from Refs. 44 ([BMIM]PF₆) and 45 (OMIM compounds). The pressure ranges from ambient to 224 MPa.

volume dependence of η . As seen in Fig. 6, the viscosity is almost constant as density is varied at constant temperature. The fact that temperature is the dominant control variable for the viscosity of strongly H-bonded liquids agrees with the general trend found for the relaxation time of various glass formers.^{17,71}

Ionic liquids

Ionic bonds are even stronger than H bonds and hence tend to yield crystalline solids of high melting point. The molten liquid state of inorganic salts often requires temperatures above 500 K, limiting experimental investigations. A feature that inorganic salts have in common with water is a propensity to form network structures^{79,80} and as discussed above, in general, we cannot expect the thermodynamic scaling to apply to network-forming liquids. A recent MDS of silica by De Michele *et al.*⁸¹ demonstrates this; isodiffusivities calculated for various thermodynamic conditions do not correspond to a constant value of TV^γ . Instead there are two regimes, due to the coupling between the density of silica and its ability to form bonds between Si and O atoms.

For compounds having ionic interactions weaker than those of the inorganic salts, network formation is suppressed and conformance to the scaling may be observed. Salts in which the cation is bulky and asymmetric can dissociate at moderate temperatures to form a viscous liquid. Viscosity measurements have been carried out at elevated pressures on three ionic liquids for which PVT data are also available.^{44,45} These materials have the typical structure of low temperature ionic liquids—a nitrogen-containing, organic cation and an inorganic anion, which poorly coordinate and thus melt at low temperature.

The viscosity data for each liquid superpose for low values of $\gamma < 3$ (Fig. 7). The dynamics primarily reflect the influence of temperature, consistent with strong intermolecular forces due to the electrostatic interactions. The smallest scal-

ing exponent, $\gamma=2.25$, is found for the [OMIM]BF₄. The tetrafluoroborate counter ion has a tetrahedral geometry and more compact size than the octahedral hexafluorophosphate: the F in BF₄ is 1.42 Å from the central atom versus 1.65 Å in PF₆.⁸² The result is a stronger effective negative charge [by about a factor of 2 (Ref. 82)] and consequently stronger electrostatic interactions in [OMIM]BF₄. The exponent is larger for [OMIM]PF₆ in comparison to [BMIM]PF₆, which we can speculate is due to increased van der Waals interactions for the bulkier cation. This size effect is seen directly in the magnitude of the viscosity, which is about threefold larger for [OMIM]PF₆ than for [BMIM]PF₆ (Fig. 7). Although this first application of the scaling to ionic liquids is successful, certainly it would be of interest to determine if limits exist at extended densities or temperatures, as seen for H-bonded materials.

CONCLUDING REMARKS

Although the rationale for the thermodynamic scaling arose originally from a consideration of intermolecular forces and their relationship to local dynamics, obviously a spherical two-body repulsive potential [Eq. (1)] can only crudely approximate the interactions between real molecules. Nevertheless, the superposition of relaxation times according to Eq. (2) is an empirical fact, having been verified now for at least 50 molecular liquids and polymers.^{17,21–32,65} The appeal of the analysis extends beyond the utility of the scaling to organize and extrapolate experimental data. The magnitude of the exponent γ provides a direct link to the manner in which molecules negotiate a complex potential energy landscape, in which density-dependent local barriers exceed the available thermal energy. Molecular motion must proceed via many-body cooperative dynamics, which evolve with changing temperature and volume. A given value of TV^γ corresponds to some average local arrangement (static structure factor).¹⁸ The scaling exponent quantifies the steepness of the intermolecular potential and thus the relative contribution of T and V . It is for this reason that a connection exists between γ and the Grüneisen parameter characterizing the anharmonicity of the potential.^{34,35}

Herein we extend the scaling to characterize the T and V dependences of the viscosity for 12 materials (Table I). For the nonpolar liquids (octane, toluene, BCH, and PFPE), γ is large (≥ 6), consistent with earlier work showing the strong effect of volume on dielectric relaxation in supercooled van der Waals molecular liquids.^{83–85} More polar interactions (as in DPEB and DBP herein) or more intramolecular bonding (squalane and mineral oil) reduces the influence of volume, thereby reducing γ . Polymer molecules exist as an extended, intramolecularly bonded structure, which reduces the number of possible rearrangements and thus generally weakens volume effects.^{17,71} For a polymer capable of H bonding such as polyglycol, the small value of $\gamma=2.3$ is likely due to the combined effects of strong interactions and chain connectivity. Usually, high molecular weight polymers, with the exception of very flexible chains such as polysiloxanes and some polyethers,^{22,31} are characterized by small values of $\gamma(<2.6)$.^{17,22} The tendency of H bonds to dissociate at higher

T or P can cause deviations from Eq. (2), since the structure of the material itself changes. This behavior is exemplified herein by water. Finally, we find that for ionic liquids, in which strong electrostatic forces are operative, the scaling exponent is small (<3). The differences in γ among the three ionic liquids analyzed herein are not large, but they are consistent with the trend of stronger attractive interactions softening the effective hardcore potential, giving rise to smaller γ .

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